



**INDIAN SCHOOL MUSCAT
HALF YEARLY EXAMINATION
MATHEMATICS**

CLASS: XI

Sub. Code: 041

Time Allotted: 3 Hrs

29.09.2019

Max. Marks: 80

General Instructions:

- (i) All questions are compulsory.
- (ii) Questions in section A are MCQ & very short answer type questions carrying 1 mark each.
- (iii) Questions in section B are short- answer type questions carrying 2 marks each.
- (iv) Questions in section C are long answer - I type questions carrying 4 marks each.
- (v) Questions in section D are long answer - II type questions carrying 6 marks each.

SECTION - A (Questions 1 to 20 carry 1 mark each)

I. CHOOSE THE CORRECT ANSWER. WRITE THE ANSWER ALONG WITH THE CORRECT OPTION: (1x10 = 10 marks)

1. If $\cos x = k$ has exactly one solution in $[0, 2\pi]$, find the value of k .
 (a) -1 (b) $\frac{1}{\sqrt{2}}$ (c) $-\frac{1}{2}$ (d) 0
2. If A, B are non-empty sets, then $(A - B) \cup (B - A)$ equals :
 (a) $(A \cup B) - B$ (b) $A - (A \cap B)$ (c) $(A \cup B) - (A \cap B)$ (d) $(A \cup B) \cup (A \cap B)$
3. If $\sum n = 210$, then the value of $\sum n^2$ is :
 (a) 2870 (b) 2160 (c) 2970 (d) 2170
4. Domain of the function $f(x) = \frac{1}{\sqrt{x+|x|}}$ is :
 (a) $[0, \infty)$ (b) $(0, \infty)$ (c) $(-\infty, \infty)$ (d) $(-\infty, 0)$
5. If S_n denotes the sum of first n terms of an A.P whose common difference is d , then $S_n - 2S_{n-1} + S_{n-2}$ ($n > 2$) is equal to :
 (a) $2d$ (b) d (c) $-d$ (d) none of these
6. Let R be a relation on N defined by $x + 2y = 8$. The domain of R is :
 (a) {2, 4, 8} (b) {2, 4, 6, 8} (c) {2, 4, 6} (d) {1, 2, 3, 4}
7. Which of the following is an empty set?
 (a) $\{x: x \in R, x^2 - 1 = 0\}$ (b) $\{x: x \in R, x^2 + 1 = 0\}$
 (c) $\{x: x \in R, x^2 - 2 = 0\}$ (d) $\{x: x \in R, x^2 - x - 2 = 0\}$

8. If $n = 10$, $\bar{x} = 12$ and $\sum x_i^2 = 1530$, then the coefficient of variation is
 (a) 36 (b) 41 (c) 25 (d) none of these
9. What is the value of $\frac{\cos 18^\circ - \sin 18^\circ}{\sin 27^\circ}$?
 (a) $\sqrt{2}$ (b) $-\sqrt{2}$ (c) $\frac{1}{\sqrt{2}}$ (d) $\frac{-1}{\sqrt{2}}$
10. Find the smallest natural number satisfying the inequality $20 - 5x < 5(x + 8)$.
 (a) -1 (b) 1 (c) 0 (d) 2

II. **ANSWER THE FOLLOWING : (1x10 = 10 marks)**

11. The marks obtained by Sukriti in first two unit tests are 75 and 70. Find the minimum marks she should get in the third test to have an average of atleast 60 marks.
12. Write the set $\left\{\frac{2}{5}, \frac{3}{7}, \frac{4}{9}, \frac{5}{11}, \frac{6}{13}\right\}$ in set-builder form.
13. Standard deviation of a collection of data is $2\sqrt{2}$. If each observation is multiplied by 3, find the variance of the new data.
14. If $A = \{x: x \in N, x < 10\}$ then find the value(s) of x for which $-3 < 3x - 1 < x + 5$.
15. Let f be a function defined by $f(x) = 5x^2 + 2$, $x \in R$. Find x such that $f(x) = 22$.
16. Find the value of $9^{1/3} \cdot 9^{1/9} \cdot 9^{1/27} \dots \dots$ upto ∞ terms.
17. Find the range of the function: $f(x) = 1 - |x - 2|$
18. If number of subsets of a set is 32, find the number of elements in the set.
19. Write the radian measure of $-47^\circ 30'$.
20. Find the value of $\tan\left(\frac{23\pi}{6}\right)$

SECTION - B (Questions 21 to 26 carry 2 marks each)

21. Find the mean deviation about the median for the following data:

x_i	10	11	12	13	14
f_i	3	12	18	12	3

22. Find the domain and range of the function $f(x) = \frac{x+2}{|x+2|}$

OR

Find the domain and range of the function $f(x) = \sqrt{x-1}$

23. If $P = \{x: x < 3, x \in N\}$ and $Q = \{x: x \leq 2, x \in W\}$, find $(P \cup Q) \times (P \cap Q)$.

24. Find the mean and variance of first n natural numbers.

OR

Find the mean and variance of first 10 multiples of 3.

25. A horse is tied to a post by a rope 30 m long. If the horse moves along the circumference of a circle always keeping the rope tight, find how far will it have gone when the rope has traced an angle of 105° .

26. If $A = \{2, 4, 6, 9\}$ and $B = \{4, 6, 18, 27\}$, find relation R defined by $R = \{(x, y) : x \text{ is a factor of } y \text{ and } x < y, x \in A, y \in B\}$.

SECTION - C (Questions 27 to 32 carry 4 marks each)

27. If a, b are the roots of $x^2 - 3x + p = 0$ and c, d are the roots of $x^2 - 12x + q = 0$, where a, b, c, d form a G.P, prove that $(q + p) : (q - p) = 17 : 15$.

28. If $\tan x = \frac{3}{4}$ and x lies in the third quadrant, find the values of $\sin \frac{x}{2}$, $\cos \frac{x}{2}$ and $\tan \frac{x}{2}$.

OR

Prove that $\frac{\cos x}{1 - \sin x} = \tan \left(\frac{\pi}{4} + \frac{x}{2} \right)$

29. Solve the equation : $\sin x + \sin 3x + \sin 5x = 0$.

30. The sum of two numbers is 6 times their geometric mean. Show that the numbers are in the ratio $(3 + 2\sqrt{2}) : (3 - 2\sqrt{2})$.

OR

Find the sum to n terms of the series: $1^2 + (1^2 + 2^2) + (1^2 + 2^2 + 3^2) + \dots$

31. Given: $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{2, 4, 6, 8\}$, $B = \{2, 3, 5, 7\}$, verify De Morgan's laws.

32. Prove by the principle of mathematical induction for all $n \in N$:

$$\frac{1}{3 \cdot 5} + \frac{1}{5 \cdot 7} + \frac{1}{7 \cdot 9} + \dots + \frac{1}{(2n+1)(2n+3)} = \frac{n}{3(2n+3)}$$

SECTION - D (Questions 33 to 36 carry 6 marks each)

33. Calculate the mean, variance and standard deviation for the following data:

Wages (in Rs)	0-10	10-20	20-30	30-40	40-50	50-60	60-70
No. of workers	9	17	32	23	40	18	1

OR

For a frequency distribution consisting of 18 observations, the mean and standard deviation were found to be 7 and 4 respectively. But on rechecking, it was found that an observation 12 was miscopied as 21 in calculations. Calculate the correct mean and standard deviation.

34. Solve the following system of inequalities graphically:
 $3y - 2x \leq 4$, $x + 3y \geq 3$, $x + y \leq 5$, $x \geq 0, y \geq 0$.

OR

A manufacturer has 600 litres of 12% solution of acid. How many litres of 30% acid solution must be added to it so that acid content in the resulting mixture will be more than 15% but less than 18% acid?

35. Prove that $\cos^2 x + \cos^2 \left(x + \frac{\pi}{3}\right) + \cos^2 \left(x - \frac{\pi}{3}\right) = \frac{3}{2}$
36. Out of 40 students, 15 passed in English, 12 passed in Mathematics and 8 passed in Science; 6 in English and Mathematics; 7 in Mathematics and Science; 4 in English and Science and 4 in all the three subjects. Find how many passed
(i) in English and Mathematics but not in Science
(ii) in Mathematics only
(iii) in more than one subject.

End of the Question Paper